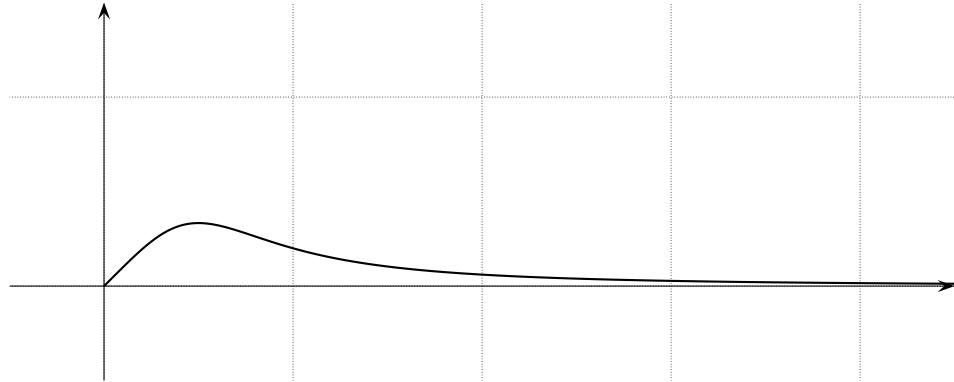


11.22 1)



$$\begin{aligned} 2) \quad & \pi \int_0^{+\infty} \left(\frac{x}{4x^3 + 1} \right)^2 dx = \pi \int_0^{+\infty} \frac{x^2}{(4x^3 + 1)^2} dx = \pi \lim_{t \rightarrow +\infty} \int_0^t \frac{x^2}{(4x^3 + 1)^2} dx \\ &= \pi \lim_{t \rightarrow +\infty} \frac{1}{12} \int_0^t (4x^3 + 1)^{-2} \cdot 12x^2 dx = \frac{\pi}{12} \lim_{t \rightarrow +\infty} \frac{1}{-1} (4x^3 + 1)^{-1} \Big|_0^t = \\ & \frac{\pi}{12} \lim_{t \rightarrow +\infty} -\frac{1}{4x^3 + 1} \Big|_0^t = \frac{\pi}{12} \lim_{t \rightarrow +\infty} \left(-\frac{1}{4t^3 + 1} + \frac{1}{4 \cdot 0^3 + 1} \right) = \\ & \frac{\pi}{12} \lim_{t \rightarrow +\infty} \left(-\frac{1}{4t^3 + 1} + 1 \right) = \frac{\pi}{12} \lim_{t \rightarrow +\infty} \left(-\frac{1}{4t^3} + 1 \right) = \frac{\pi}{12} (-0 + 1) = \frac{\pi}{12} \end{aligned}$$