

2.15 1) $5^x = 25$

$$5^x = 5^2$$

$$x = 2$$

$$S = \{2\}$$

2) $3^x = \frac{1}{9}$

$$3^x = \frac{1}{3^2}$$

$$3^x = 3^{-2}$$

$$x = -2$$

$$S = \{-2\}$$

3) $2^x = \frac{1}{8}$

$$2^x = \frac{1}{2^3}$$

$$2^x = 2^{-3}$$

$$x = -3$$

$$S = \{-3\}$$

4) $4^x = 64$

$$4^x = 4^3$$

$$x = 3$$

$$S = \{3\}$$

5) $4^x = 8$

$$(2^2)^x = 2^3$$

$$2^{2x} = 2^3$$

$$2x = 3$$

$$x = \frac{3}{2}$$

$$S = \{\frac{3}{2}\}$$

6) $25^x = 125$

$$(5^2)^x = 5^3$$

$$5^{2x} = 5^3$$

$$2x = 3$$

$$x = \frac{3}{2}$$

$$S = \{\frac{3}{2}\}$$

7) $16^x = 64$

$$(2^4)^x = 2^6$$

$$2^{4x} = 2^6$$

$$4x = 6$$

$$x = \frac{6}{4} = \frac{3}{2}$$

$$S = \{\frac{3}{2}\}$$

$$\begin{aligned}
 8) \quad & 3^x = 9^{2x+3} \\
 & 3^x = (3^2)^{2x+3} \\
 & 3^x = 3^{2(2x+3)} \\
 & 3^x = 3^{4x+6} \\
 & x = 4x + 6 \\
 & 0 = 3x + 6 \\
 & x = -2 \\
 & S = \{-2\}
 \end{aligned}$$

$$\begin{aligned}
 9) \quad & 3^{3x+2} = 9^x \\
 & 3^{3x+2} = (3^2)^x \\
 & 3^{3x+2} = 3^{2x} \\
 & 3x + 2 = 2x \\
 & x + 2 = 0 \\
 & x = -2 \\
 & S = \{-2\}
 \end{aligned}$$

$$\begin{aligned}
 10) \quad & 9^{2x+1} = 1 \\
 & 9^{2x+1} = 9^0 \\
 & 2x + 1 = 0 \\
 & x = -\frac{1}{2} \\
 & S = \{-\frac{1}{2}\}
 \end{aligned}$$

$$\begin{aligned}
 11) \quad & 2^x - 16 \cdot 2^{3x+2} = 0 \\
 & 2^x = 16 \cdot 2^{3x+2} \\
 & 2^x = 2^4 \cdot 2^{3x+2} \\
 & 2^x = 2^{4+3x+2} \\
 & x = 4 + 3x + 2 \\
 & -2x = 6 \\
 & x = -3 \\
 & S = \{-3\}
 \end{aligned}$$

$$\begin{aligned}
 12) \quad & 16 \cdot 2^x = 4^{3x+5} \\
 & 2^4 \cdot 2^x = (2^2)^{3x+5} \\
 & 2^{4+x} = 2^{2(3x+5)} \\
 & 4 + x = 2(3x + 5) = 6x + 10 \\
 & -5x = 6 \\
 & x = -\frac{6}{5} \\
 & S = \{-\frac{6}{5}\}
 \end{aligned}$$

$$\begin{aligned}
 13) \quad & 5^{3x+2} - \frac{1}{25} = 0 \\
 & 5^{3x+2} = \frac{1}{25}
 \end{aligned}$$

$$5^{3x+2} = 5^{-2}$$

$$3x + 2 = -2$$

$$3x = -4$$

$$x = -\frac{4}{3}$$

$$S = \left\{-\frac{4}{3}\right\}$$

$$14) \quad 2^{x+7} = 4^{5x+2}$$

$$2^{x+7} = (2^2)^{5x+2}$$

$$2^{x+7} = 2^{2(5x+2)}$$

$$x + 7 = 2(5x + 2) = 10x + 4$$

$$-9x = -3$$

$$x = \frac{1}{3}$$

$$S = \left\{\frac{1}{3}\right\}$$

$$15) \quad 7^{8x^2+4} = 7^{(2-3x)^2}$$

$$8x^2 + 4 = (2 - 3x)^2$$

$$8x^2 + 4 = 4 - 12x + 9x^2$$

$$0 = x^2 - 12x = x(x - 12)$$

$$x = 0 \quad \text{ou} \quad x = 12$$

$$S = \{0; 12\}$$

$$16) \quad 11^{x^2+3} = 11^{2x^2-6}$$

$$x^2 + 3 = 2x^2 - 6$$

$$0 = x^2 - 9 = (x + 3)(x - 3)$$

$$x = -3 \quad \text{ou} \quad x = 3$$

$$S = \{-3; 3\}$$

$$17) \quad 3^{2x} (3^x - 3)^2 = 0$$

$$3^{2x} = 0 \quad \text{ou} \quad 3^x - 3 = 0$$

(a) $3^{2x} = 0$ n'admet aucune solution, car $3^y > 0$ pour tout $y \in \mathbb{R}$.

(b) $3^x - 3 = 0$

$$3^x = 3 = 3^1$$

$$x = 1$$

$$S = \{1\}$$

$$18) \quad 2^{x^2} = 4 \cdot 2^x$$

$$2^{x^2} = 2^2 \cdot 2^x$$

$$2^{x^2} = 2^{2+x}$$

$$x^2 = 2 + x$$

$$x^2 - x - 2 = (x + 1)(x - 2) = 0$$

$$x = -1 \quad \text{ou} \quad x = 2$$

$$S = \{-1; 2\}$$

$$\begin{aligned}19) \quad & 2^{x^2} \cdot 4^x = 8 \\& 2^{x^2} \cdot (2^2)^x = 2^3 \\& 2^{x^2} \cdot 2^{2x} = 2^3 \\& 2^{x^2+2x} = 2^3 \\& x^2 + 2x = 3 \\& x^2 + 2x - 3 = (x+3)(x-1) = 0 \\& x = -3 \quad \text{ou} \quad x = 1 \\& S = \{-3; 1\}\end{aligned}$$

$$\begin{aligned}20) \quad & 10^x = 1000^{2x-2} \\& 10^x = (10^3)^{2x-2} \\& 10^x = 10^{3(2x-2)} \\& x = 3(2x-2) = 6x-6 \\& 0 = 5x-6 \\& x = \frac{6}{5} \\& S = \left\{\frac{6}{5}\right\}\end{aligned}$$